## Search

INTRODUCTION TO

## ARTIFICIAL INTELLIGENCE

BIL 472
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## Administration

Short written homeworks each week First one today
Web page is up
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## What's AI? (to me)

Computers making decisions in real-world problems


## Search Problems

Let $s$ be the set of states (strings)
Input:

- Initial state: $\mathrm{s}_{\mathrm{o}}$
- Neighbor generator, $\mathrm{N}: S \rightarrow 2^{s}$
- Goal function, G: $S \rightarrow\{0,1\}$


## Search Answer

 $\mathrm{s}_{1}, \ldots, \mathrm{~S}_{\mathrm{n}}$ such that:- $\mathrm{s}_{1}, \ldots, \mathrm{~s}_{\mathrm{n}} \in S$
- for all $1 \leq i \leq n, s_{i} \in N\left(s_{i-1}\right)$
- $G\left(s_{n}\right)=1$


## Examples

We're very impressed. Meaning?

- Rush Hour
- 8-puzzle
- Logistics
- 8-queens problem
- Logic puzzles
- Job-shop scheduling


## Rush Hour

Move cars forward and backward to "escape"


## Search Version

States: configurations of cars
$\mathrm{N}(\mathrm{s})$ : reachable states
G(s): 1 if red car at gate


## 8-puzzle

## Slide tiles into order

States:
$\mathrm{N}(\mathrm{s}):$

G(s):


## Logistics

Very sophisticated. What goes where when?

Desert Storm logistics "paid for AI research"


## 8 Queens Puzzle

No captures

## States:

$\mathrm{N}(\mathrm{s}):$

G(s):


## Logic Puzzles

1. Jody, who is an ape, wasn't the ape who returned immediately after Tom and immediately before the animal who appeared in the movie with no rating.
2. The only lions that were used in the movies were the one who was the third to return, the one who appeared in the R movie, and the one who appeared in "Luck". ...

## Job-Shop Scheduling

Industrial problem:

- Allocate machines and machinists to time slots
- Constraints on orders in which parts are serviced



## Search Template

- fringe $=\left\{\left(\mathrm{s}_{\mathrm{o}}, \mathrm{o}\right)\right\} ; / *$ initial cost */
- markvisited $\left(\mathrm{s}_{0}\right)$;
- While (1) \{

If empty(fringe), return failure;
( $\mathrm{s}, \mathrm{c}$ ) = removemincost(fringe);
If $\mathrm{G}(\mathrm{s})$ return s ;
Foreach s' in N(s)
if unvisited(s') fringe = fringe $\mathrm{U}\left\{\left(\mathrm{s}^{\prime}, \operatorname{cost}\left(\mathrm{s}^{\prime}\right)\right\}\right.$; markvisited $\left(\mathrm{s}_{0}\right)$;
\}

## Data Structures

How implement this efficiently?

- removemincost-U-empty?
- markvisited-unvisited?


## Vary Cost

How does search behavior change with cost?

- $\operatorname{cost}\left(s^{\prime}\right)=c+1$
- $\operatorname{cost}\left(s^{\prime}\right)=c-1$


## Grid Example: BFS



## Grid Example: DFS O



## How Evaluate?

## What makes one search scheme better than another?

- Completeness: Find solution?
- Time complexity: How long?
- Space complexity: Memory?
- Optimality: Find shortest path?


## Depth vs. Breadth-first

Let $|\mathrm{T}(\mathrm{s})| \leq \mathrm{b}$ (branching factor), goal at depth d

- How implement priority queue?
- Completeness?
- Time complexity?
- Space complexity?
- Optimality?


## BFS

- Completeness?
- Yes
- Time complexity? - O(bl)
- Space complexity?
- O(bd) ${ }^{\text {d }}$
- Optimality?
- yes


## DFS

- Completeness?
- Yes, assuming state space finite
- Time complexity?
- O(|S|), can do well if lots of goals
- Space complexity?
- O(n), n deepest point of search
- Optimality?
- No :


## Depth-limited Search

DFS, only expand nodes depth $\leq 1$.

- Completeness?
- No, if l $\leq \mathrm{d}$. :
- Time complexity?
- O(bl$)$
- Space complexity?
- O(l)
- Optimality?
- No :


## Iterative Deepening

Depth limited, increasing l.

- Completeness?
- Yes.
- Time complexity?
$\circ$ O(bd), even with repeated work! ©
- Space complexity?
- O(d)
- Optimality?
- Yes


## Bidirectional Search

BFS in both directions
Need $\mathrm{N}^{-1}$
How could this help?

- $b^{1}$ VS 2bl/2

What makes this hard to implement?

## Which do you choose?

- 8-queens, neighbors of $s$ add one queen to board



## Which do you choose?

- Big grid, goal nearby



## What to Learn

How to express problems in the search framework The basic algorithms for search
Strengths and weaknesses of the basic algorithms

## Homework 1 (due 16 Feb 2015)

1. Get involved into AI course content (web, e-mail or facebook)
2. Let BFS' and DFS' be versions of BFS and DFS that don't check whether a state has been previously visited. Evaluate BFS' and DFS' on the four comparison criteria we discussed.
3. Consider the Rush Hour board from these notes. Assume a single move consists of sliding a car forward or backward some number of spaces. (a) Give an upper bound on the branching factor. (b) Assuming the solution is at depth 20, how many nodes will be searched? (c) Ignoring the search, how many states are in the search space? Give as tight an upper bound as you can.
